Dr. Marques Sophie Office 519 Linear algebra

Spring Semester 2013 marques@cims.nyu.edu

## Problem Set #2

## Due Tuesday 18 february in Class

## Exercise 1 ( $\star$ ):

Let  $M_{n \times n}(K)$  be the space of the square matrices with n rows and n columns.

- 1. Prove that the product of two upper triangular matrices is upper triangular and the same fact for strictly upper triangular matrices.
- 2. Prove that a strictly upper triangular matrix A is nilpotent:  $A^n = A \times \dots \times A(ntimes) = 0.$

## [F] FOURTH EDITION :

- Section 1.4 Exercises 14 and 15
- Section 1.6 Exercises 8 and 13.

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 $<sup>^{1}(\</sup>star) = \text{easy}$ ,  $(\star\star) = \text{medium}$ ,  $(\star\star\star) = \text{challenge}$